

Read Unit 3 (*SRQM by Ruler&Compass*) thru page 28. Study Lecture 25-26

Space-time and per-space-time

Lorentz-Minkowski space-time (or per-space-time) coordinate system graphs (similar to the ones made in class for $u = \frac{3}{5}c$) are attached and available on-line. Let 1 inch squares correspond to (*light-sec., sec.*) in space-time (x, ct) or to the per-space-time units (*light-Hz, Hz*) on a (κ, ν) graph. Space-time graphs for the problems below require ± 5 values for space and time. Graphs can be flipped so either Lighthouse or else Ship can have square (rest frame) axes. You should do one of each.

NOTE: For this assignment it is recommended you follow the Newtonian graph convention: +x-to-the-right and +ct-down. This conforms to the animations on two of our main relativity web apps: *Pirelli Relativity Challenge* and *RelativIt*.

Follow these links to go to them directly:

- http://www.uark.edu/ua/pirelli/html/lighthouse_scenarios.html
- <http://www.uark.edu/ua/modphys/markup/RelativItWeb.html?scenario=22>
- <http://www.uark.edu/ua/modphys/markup/RelativItWeb.html?scenario=24>

Space-time Terrorism

1 (a) Complete the following happening tables using the Lorentz transformation between ship space-time coordinates (x', ct') and lighthouse coordinates (x, ct) given that the ship is traveling from right to left at a speed of $u = \frac{3}{5}c$ and passes the lighthouse at $t=0=t'$. Calculate answers needed below by algebra and then make a $u = \frac{3}{5}c$ plot to check the results.

Ship emits light	Explosion #1	Explosion #2	Explosion #3
x = 3 litesec. t = -5 sec.	x = t =	x = -1 litesec. t = -1 sec.	x = t = 1 sec.
x' = t' =	x' = -1 litesec. t' = -3 sec.	x' = t' =	x' = -3 litesec. t' =

Draw the space-time paths of light waves emitted right and left from explosions #1 and #2 on the space-time graph and answer the following questions.

If lighthouse broadcasts 100 Mhz what ν does ship tune to receive it at $t=-1$? MHz at $t=+1$? Mhz

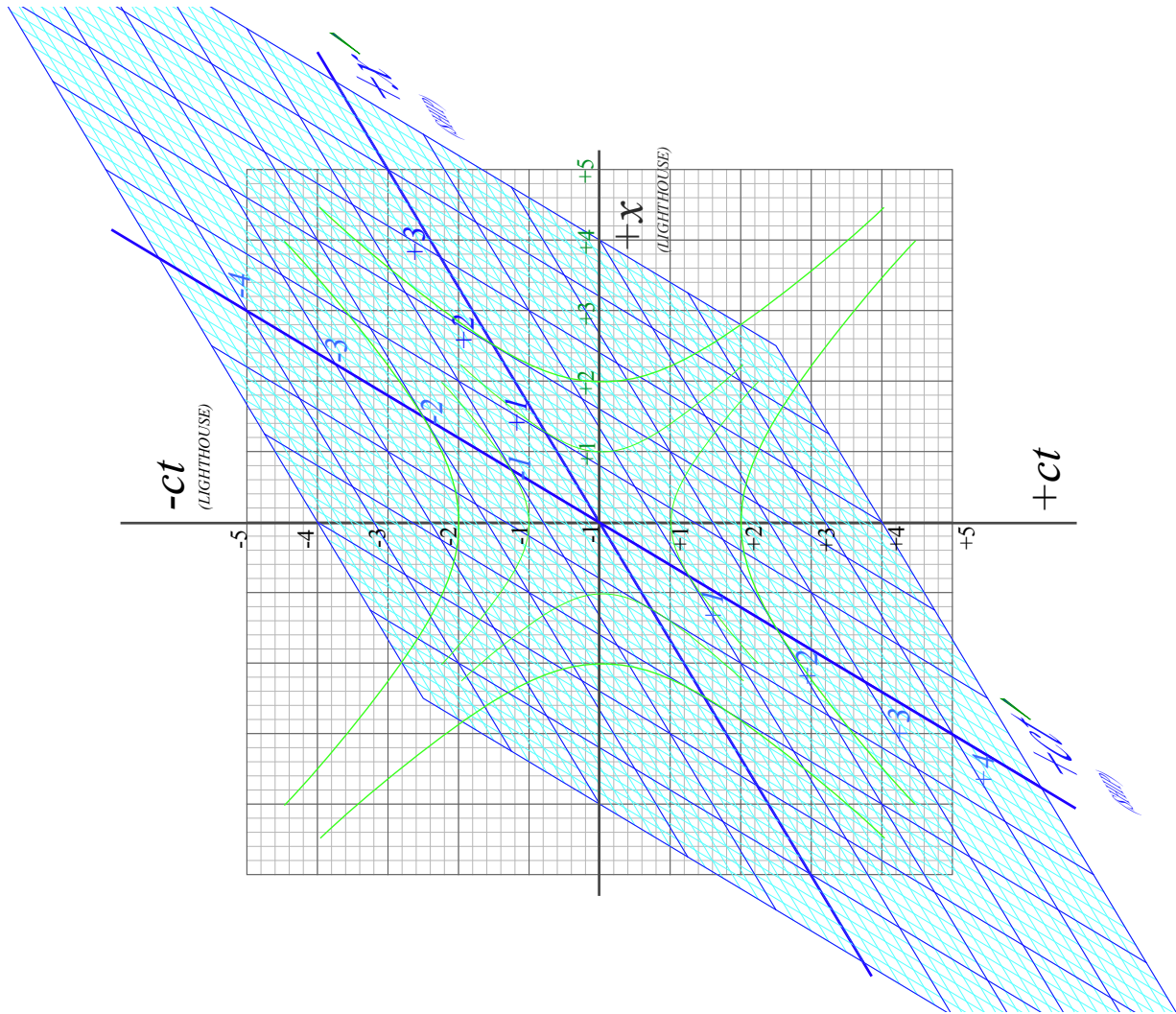
- (a) What is rapidity of ship relative to lab $\rho_{SvsL} = \underline{\hspace{2cm}}$? ... lab relative to ship $\rho_{LvsS} = \underline{\hspace{2cm}}$?
- (b) When does light from explosion #1 hit the lighthouse? (Lighthouse time)
- (c) When does light from explosion #1 hit the lighthouse? (Ship time)
- (d) When does light from explosion #2 hit the lighthouse? (Lighthouse time)
- (e) When does light from explosion #2 hit the lighthouse? (Ship time)
- (f) Draw paths of fragments from explosions #1 and #2 for fragment speed $c/2$ or $-c/2$ relative to the ship.

B.I.G.A.N.N. Investigates

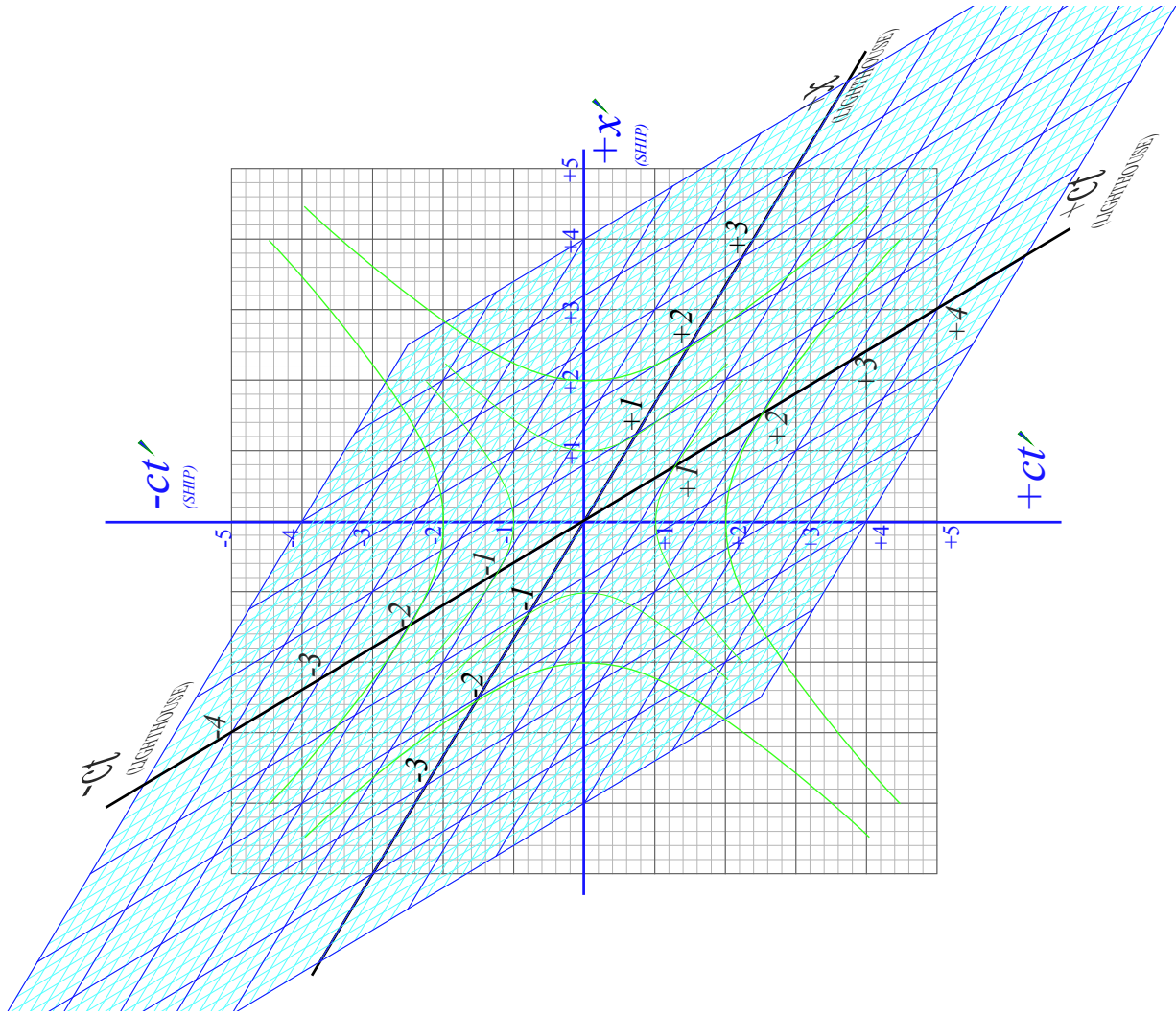
2 Explosions in problem 1 lead to an investigation by B.I.G.A.N.N. (Bureau of Intergalactic Aids to Navigation at Night) .

- (a) When does the first fragment from explosion #1 hit the lighthouse? (Lighthouse time)
- (b) When does a second fragment from explosion #1 hit the lighthouse? (Lighthouse time)
- (c) When does a fragment from explosion #1 hit the ship? (Ship time)
- (d) When does a fragment from explosion #2 hit the ship? (Ship time)
- (e) When does a fragment from explosion #2 hit the Lighthouse? (Lighthouse time)
- (f) ...lighthouse says 1st fragment goes c using **addition formula of rapidity** $\rho_{FvsL} = \rho_{FvsS} + \rho_{SvsL}$ and of **velocity**:
- (g) ...lighthouse says 2nd fragment goes c

The authorities of BIGANN have spotted a causal (as opposed to acausal) connection between all the explosions. To whom does it point?



Better version of Lighthouse-square graph available in class or online.



Better version of Ship-square graph available in class or online.