Principles of Symmetry, Dynamics, and Spectroscopy
- W. G. Harter - Wiley (1993)

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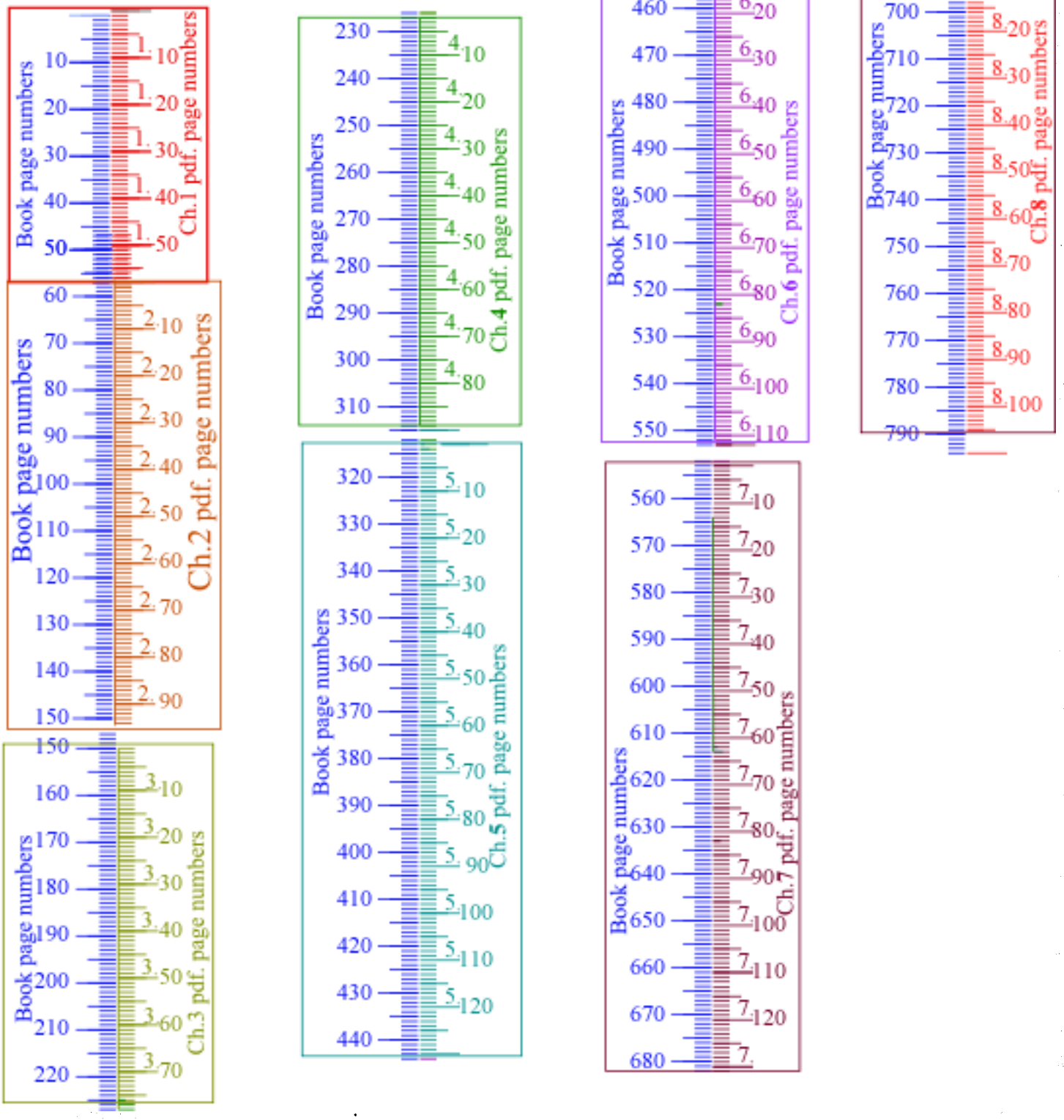

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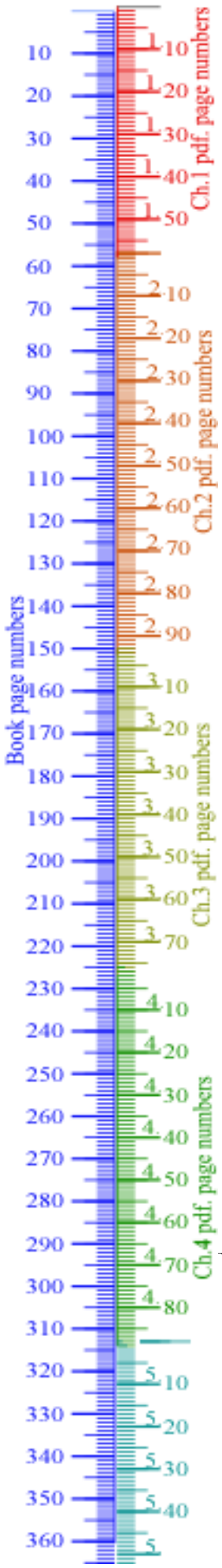

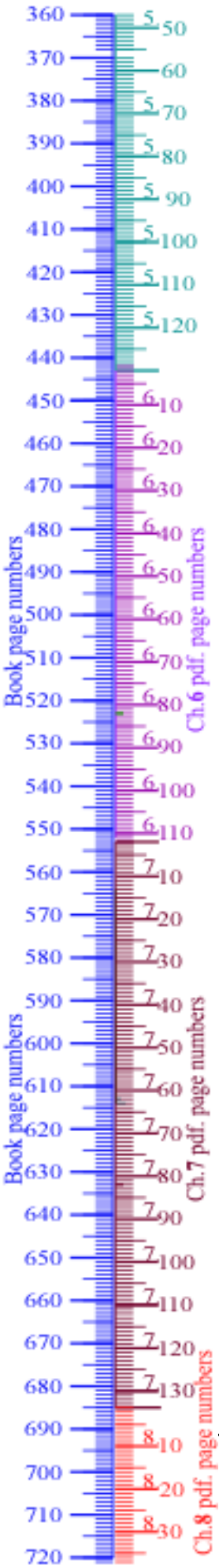

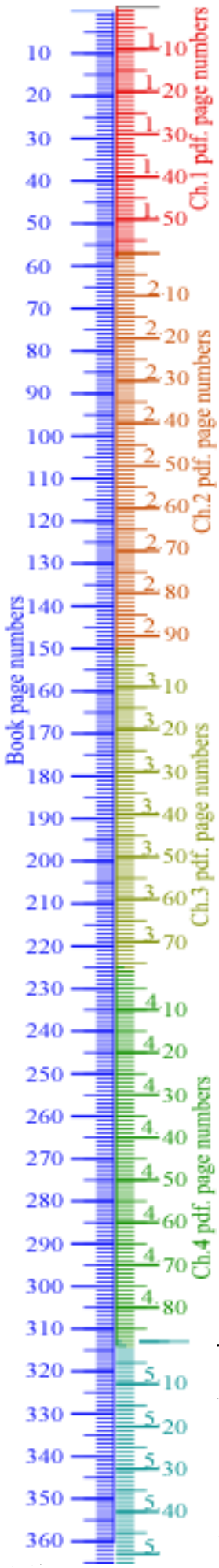

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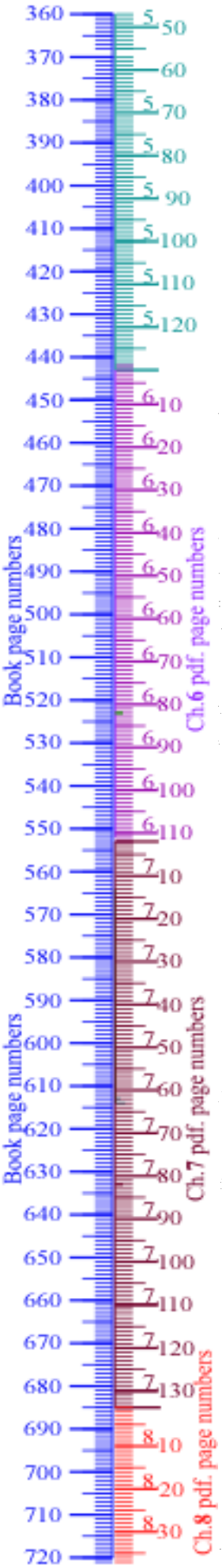

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